## SRI KRISHNA INSTITUTE OF TECHNOLOGY,BANGALORE



COURSE PLAN
Academic Year 2019-20

| Program: | BS |
| :---: | :---: |
| Semester: | 4 |
| Course Code: | 18MAT41 |
| Course Title: | COMPLE ANALYI,PROBABILITY\&TATITICAL |
| METHODS |  |

## Academic Evaluation and Monitoring Cell

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## Table of Contents

A. COURSE INFORMATION ..... 3

1. Course Overview. ..... 3
2. Course Content ..... 3
3. Course Material ..... 4
4. Course Prerequisites ..... 5
5. Content for Placement, Profession, HE and GATE ..... 5
B. OBE PARAMETERS ..... 5
6. Course Outcomes ..... 5
7. Course Applications ..... 6
8. Mapping And Justification. ..... 7
9. Articulation Matrix ..... 9
10. Curricular Gap and Content. ..... 10
11. Content Beyond Syllabus ..... 10
C. COURSE ASSESSMENT ..... 10
12. Course Coverage ..... 10
13. Continuous Internal Assessment (CIA) ..... 10
D1. TEACHING PLAN - 1 ..... 11
Module - 1 ..... 11
Module - 2 ..... 13
E1. CIA EXAM - 1 ..... 13
a. Model Question Paper - 1 ..... 13
b. Assignment -1 ..... 14
D2. TEACHING PLAN - 2 ..... 16
Module - 3 ..... 16
Module - 4 ..... 17
E2. CIA EXAM - 2. ..... 19
a. Model Question Paper - 2 ..... 19
b. Assignment - 2 ..... 19
D3. TEACHING PLAN - 3 ..... 20
Module - 5 ..... 20
E3. CIA EXAM - 3 . ..... 22
a. Model Question Paper - 3 ..... 22
b. Assignment - 3 ..... 23
F. EXAM PREPARATION ..... 24
14. University Model Question Paper. ..... 24
15. SEE Important Questions ..... 25
G. Content to Course Outcomes ..... 27
16. TLPA Parameters ..... 27
17. Concepts and Outcomes ..... 28
Note : Remove "Table of Content" before including in CP BookEach Course Plan shall be printed and made into a book with cover pageBlooms Level in all sections match with A.2, only if you plan to teach / learn at higher levels

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## A. COURSE INFORMATION

## 1. Course Overview

| Degree: | BE | Program: | ME/CV/ECE/CSE/I <br> SE/EEE |
| :--- | :--- | :--- | :--- |
| Year / Semester: | IV | Academic Year: | 2019-20 |
| Course Title: | Complex Analysis, Probability And <br> Statistical Methods | Course Code: | 18MAT41 |
| Credit / L-T-P: | $3 / 2: 2: 0$ | SEE Duration: | 180 Minutes |
| Total Contact Hours: | 50 | SEE Marks: | 60 Marks |
| CIA Marks: | 40 | Assignment | $1 /$ Module |
| Course Plan Author: | PUJITHA G | Sign | Dt: 10-02-2020 |
| Checked By: |  | Sign | Dt: |
|  |  |  |  |

Note: Define CIA and SEE \% targets based on previous performance.

## 2. Course Content

Content / Syllabus of the course as prescribed by University or designed by institute. Identify 2 concepts per module as in G .

| Mod ule | Content | Teachi ng Hours | Identified Module Concepts | Blooms Learning Levels |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Complex Variables: Review of a function of a complex variable, limits, continuity, differentiability. Analytic functions-CauchyRiemann equations in cartesian and polar forms. Properties and construction of analytic functions. | 10 | Analytic functions | L3 |
| 2 | Conformal transformations, discussion of transformations $W=\left(z^{2}\right) \quad W=e^{z}$ and bilinear transformations-problems.Complex line integrals-Cauchy's theorem andCauchy's integral formula, <br> Residues.poles.Cauchy's Residue theorem ( without proof) and problems. | 10 | Integrals and complex analysis | L4 |
| 3 | Probability Distributions: Random variables (discrete and continuous), <br> probability mass/density functions. Binomial distribution, Poisson distribution. Exponential and normal distributions, problems. | 10 | Random variables | L3 |
| 4 | curve fitting ,Statistical methods, lines of regression, correlation , rank correlation. | 10 | Data analyzing | L3 |
| 5 | Joint probability distribution: Joint Probability distribution for two discrete random variables, expectation, covariance, correlation coefficient. <br> Sampling Theory: Sampling, Sampling distributions, standard error, test of hypothesis for means and proportions, confidence limits for means, student's t-distribution, Chisquare distribution as a test of goodness of fit. | 10 | Discrete random variables. Sampling distribution in accepting or rejecting the hypothesis. | L3 |
| - | Total | 50 | - | - |

## 3. Course Material

Books \& other material as recommended by university ( $A, B$ ) and additional resources used by course teacher (C).

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1. Understanding: Concept simulation / video ; one per concept ; to understand the concepts ; $15-30$ minutes
2. Design: Simulation and design tools used - software tools used ; Free / open source
3. Research: Recent developments on the concepts - publications in journals; conferences etc.

| $\begin{gathered} \text { Modul } \\ \text { es } \end{gathered}$ | Details | Chapters in book | Availability |
| :---: | :---: | :---: | :---: |
| A | Text books (Title, Authors, Edition, Publisher, Year.) | - | - |
| 1 | B.S.Grewal: Higher Engineering Mathematics, Khanna publishers, $43^{\text {rd }}$ Ed. 2015 . |  | In Dept |
| 2 | E.Kreyszig: Advanced Engineering Mathematics,John Wiley \& Sons, $10^{\text {th }}$ Ed. (Reprint),2016. |  | In Dept |
| B | Reference books (Title, Authors, Edition, Publisher, Year.) |  |  |
| 1 | C Ray Wylie, Louis C Barrett: "Advanced Engineering Mathematics",6th Edition, 2.McGraw-Hill Book Co.,New york,1995. |  | Not Available |
| 2 | James Stewart:"Calculus- Early Transcendentals", Cengage Learning India Private Ltd. 2017. |  | Not Available |
| 3 | B.V.Ramana:"Higher Engineering Mathematics" $11^{\text {th }}$ Edition Tata McGrawHill,2010. |  | In Dept |
| 4 | Srimanta Pal \& Subobh C Bhunia: "Engineering Mathematics", Oxford UniversityPress, $3^{\text {rd }}$ Reprint, 2016. | - | Not Available |
| 5 | Gupta C B, Singh S R and Mukesh Kumar:"Engineering Mathematics for Semesterl and II, Mc-Graw Hill Education(India)Pvt.Ltd., 2015. |  | Not Available |
| D | Software Tools for Design | - | - |
|  |  |  |  |
|  |  |  |  |
| E | Recent Developments for Research | - | - |
|  |  |  |  |
| F | Others (Web, Video, Simulation, Notes etc.) | - | - |
| 1 | 01. https:// youtu.be/fOGaD2p-x3c 02. https://youtu.be/AvFs2zi3450 03. https://youtu.be/pB41_cA8zck 04. https://youtu.be/IskNRQdSWXo 05. https://youtu.be/EVPb2GWb-Rc o6. https://youtu.be/5WCDuGkj_Fw 07. https:// youtu.be/XJYdcNiHHxo 08. https://youtu.be/6ZCW/dyrRRKw 09. https:// youtu.be/CFBYX-9ywlw |  |  |
| 2 | 1. https://nptel.ac.in/courses/111107056/ |  |  |
| 3 | 1. https://nptel.ac.in/courses/111105041/ <br> 2.https://nptel.ac.in/content/storage2/nptel_data3/html/mhrd/ict/text /105105045/lec7.pdf <br> 3.https://nptel.ac.in/content/storage2/nptel_data3/html/mhrd/ict/text /103106112/lec5.pdf |  |  |
| 4 | https://www.youtube.com/watch?v=AzroLr1XS5E |  |  |
|  | https://www.youtube.com/watch? v=0WejWgMiTGg |  |  |
| 5 | https://www.youtube.com/watch? $\mathrm{l}=$ LSIgQHobj74 |  |  |
|  | https:// wwww.youtube.com/watch?v=TvCzRW/hfUk |  |  |
| G | Web links and Video Lectures: |  |  |
| 1 |  |  |  |
| 2 | VTU EDUSAT PROGRAMME - 20 |  |  |

## 4. Course Prerequisites

Refer to GL01. If prerequisites are not taught earlier, GAP in curriculum needs to be addressed. Include in Remarks and implement in B. 5 .
Students must have learnt the following Courses / Topics with described Content.

| $\begin{array}{\|c\|} \hline \text { Mod } \\ \text { ules } \end{array}$ | Course Code | Course Name | Topic / Description | Sem | Remarks | Blooms Level |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | 18MAT41 | Complex analysis,probab | Calculus of complex function | M3 | Knowledge of analytic functions | L2 |



## 5. Content for Placement, Profession, HE and GATE

The content is not included in this course, but required to meet industry \& profession requirements and help students for Placement, GATE, Higher Education, Entrepreneurship, etc. Identifying Area / Content requires experts consultation in the area.
Topics included are like, a. Advanced Topics, b. Recent Developments, c. Certificate Courses, d. Course Projects, e. New Software Tools, f. GATE Topics, g. NPTEL Videos, h. Swayam videos etc.

| Mod <br> ules | Topic / Description | Area | Remarks | Blooms <br> Level |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Calculus of complex function | HE |  | L |
| 2 | Conformal transformation\&complex <br> integration | HE |  | L 4 |
| 3 | probability | HE |  | L 6 |
| 4 | Curve fitting\&staistical methods | HE | L |  |
| 5 | Joint probability\&sampling theory | HE |  | L 4 |
| - |  |  |  |  |

## B. OBE PARAMETERS

## 1. Course Outcomes

Expected learning outcomes of the course, which will be mapped to POs. Identify a max of 2 Concepts per Module. Write 1 CO per Concept.

| Mod <br> ules Course <br> Code.\# Course Outcome <br> At the end of the course, student <br> should be able to... Teach. <br> Hours Concept Instr <br> Method Assessme <br> nt <br> Method Blooms' <br> Level <br> 1 18 MAT41 Apply the knowledge of complex <br> analysis its properties and <br> construction of analytical functions. 10 Analytic <br> functions Lecture Assignme <br> nt and <br> slip test L3 <br> 2,4 18 MAT41 Analyze various transformations to <br> convert one plane to another <br> evaluate complex integral and <br> finding the bet relation between <br> the variables. 10  Integrals <br> and <br> complex <br> analysis Lecture Assignme <br> nt and <br> slip test |
| :--- |


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| :--- |
| 3 |
| 18 MAT41 |

## 2. Course Applications

Write 1 or 2 applications per CO.
Students should be able to employ / apply the course learnings to ...

| Mod <br> ules | Application Area <br> Compiled from Module Applications. | CO | Level |
| :---: | :---: | :---: | :---: |
| 1 | To study the nature of electromagnetic wave in conductors.. | $\mathrm{co1}$ | L 3 |
| 2 | To study the nature of complex potential in field theory Curve fitting is the process <br> of constructing a curve that has the best fit to a series of data points. | $\mathrm{co2}$ | $\mathrm{~L} 3 \& \mathrm{~L} 4$ |
| 3 | To analyze problems associated with optimization of digital circuits | $\mathrm{co3}$ | L 3 |
| 4 | To solve problems related to information and coding theory\&To smoothen and <br> prediction of discrete data in digital computers \& cruise control system in motor <br> vehicles. | $\mathrm{co4}$ | L 3 |

## 3. Mapping And Justification

CO - PO Mapping with mapping Level along with justification for each CO-PO pair.
To attain competency required (as defined in POs) in a specified area and the knowledge \& ability required to accomplish it.

| Mod ules | Mapping |  | Mapping Level | Justification for each CO-PO pair | $\begin{gathered} \mathrm{Lev} \\ \mathrm{el} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| - | CO | PO | - | 'Area': ‘Competency' and 'Knowledge' for specified 'Accomplishment’ |  |
| 1 | CO1 | PO1 | 3 | Apply the knowledge of Complex Variables in finding the solution to complex engineering problems. | L3 |
| 1 | CO1 | PO 2 | 3 | Formulate engineering problems using first principles of Complex Variables. | L3 |
| 1 | CO1 | PO8 | 2 | Apply ethical principles and commit to professional ethics and responsibilities and norms of the engineering practice. | L3 |
| 1 | CO1 | PO 9 | 3 | Function effectively as an individual in multidisciplinary settings using Complex Variables . | L3 |
| 1 | CO1 | PO10 | 3 | Communicate effectively on complex engineering activities with the engineering community and with society at large such as being able to comprehend and write effective reports and design documentation make effective presentation and give and receive clear instructions. | L3 |
| 1 | CO1 | PO12 | 3 | Recognize the need for life- long learning with practical applications in engineering field using Complex Variables . | L3 |
| 2,4 | CO 2 | PO1 | 3 | Apply the knowledge of Statistical methods in finding the solution to complex engineering problems. | $\begin{gathered} \mathrm{L} 3 \& \\ \mathrm{~L} 4 \end{gathered}$ |
| 2,4 | CO 2 | PO 2 | 3 | Formulate and review engineering problems using first principles of Statistical methods. | $\begin{gathered} \mathrm{L} 3 \& \\ \mathrm{~L} 4 \end{gathered}$ |
| 2,4 | CO 2 | PO 3 | 2 | Develop and Design solutions for complex engineering problems using Statistical methods | $\begin{gathered} \mathrm{L} 3 \& \\ \mathrm{~L} 4 \end{gathered}$ |
| 2,4 | CO 2 | PO8 | 2 | Apply ethical principles and commit to professional ethics and |  |


|  |  |  |  | responsibilities and norms of the engineering practice. | L4 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 2,4 | CO 2 | PO 9 | 3 | Function effectively as an individual in multidisciplinary settings using Statistical methods. | $\begin{gathered} \mathrm{L} 3 \& \\ \mathrm{~L} 4 \end{gathered}$ |
| 2,4 | CO 2 | PO10 | 3 | Communicate effectively on complex engineering activities with the engineering community and with society at large such as being able to comprehend and write effective reports and design documentation make effective presentation and give and receive clear instructions. | $\begin{gathered} \mathrm{L} 3 \& \\ \mathrm{~L} 4 \end{gathered}$ |
| 2,4 | CO 2 | PO12 | 3 | Recognize the need for life- long learning with practical applications in engineering field using Statistical methods . | $\begin{gathered} \mathrm{L} 3 \& \\ \mathrm{~L} 4 \end{gathered}$ |
| 3 | CO 3 | PO1 | 3 | Apply the knowledge of Probability Distributions in finding the solution to complex engineering problems. | L3 |
| 3 | CO 3 | PO 2 | 2 | Formulate engineering problems using first principles of Probability Distributions. | L3 |
| 3 | CO 3 | PO8 | 3 | Apply ethical principles and commit to professional ethics and responsibilities and norms of the engineering practice. | L3 |
| 3 | CO 3 | POg | 3 | Function effectively as an individual in multidisciplinary settings using Probability Distributions. | L3 |
| 3 | $\mathrm{CO}_{3}$ | PO10 | 3 | Communicate effectively on complex engineering activities with the engineering community and with society at large such as being able to comprehend and write effective reports and design documentation make effective presentation and give and receive clear instructions. | L3 |
| 3 | CO 3 | PO12 | 3 | Recognize the need for life- long learning with practical applications in engineering field using Probability Distributions. | L3 |
| 5 | CO 4 | PO1 | 3 | Apply the knowledge of Sampling Theory in finding the solution to complex engineering problems. | L3 |
| 5 | CO 4 | PO 2 | 3 | Formulate engineering problems using first principles of Sampling Theory | L3 |
| 5 | CO4 | PO8 | 3 | Apply ethical principles and commit to professional ethics and responsibilities and norms of the engineering practice. | L3 |
| 5 | CO 4 | PO9 | 2 | Function effectively as an individual in multidisciplinary settings using Sampling Theory . | L3 |
| 5 | CO 4 | PO10 | 3 | Communicate effectively on complex engineering activities with the engineering community and with society at large such as being able to comprehend and write effective reports and design documentation make effective presentation and give and receive clear instructions. | L3 |
| 5 | CO 4 | PO12 | 4 | Recognize the need for life- long learning with practical applications in engineering field using Sampling Theory . | L3 |

## 4. Articulation Matrix

CO - PO Mapping with mapping level for each CO-PO pair, with course average attainment.

| - | - | Course Outcomes | Program Outcomes |  |  |  |  |  |  |  |  |  |  |  |  | - |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Mod ules | CO.\# | At the end of the course student should be able to . | $\begin{gathered} \mathrm{PO} \\ 1 \end{gathered}$ |  |  | $\begin{gathered} \mathrm{PO} \\ 4 \end{gathered}$ | $\begin{gathered} \mathrm{PO} \\ 5 \end{gathered}$ | $\begin{gathered} \mathrm{PO} \\ 6 \end{gathered}$ | $\begin{gathered} \mathrm{PO} \\ 7 \end{gathered}$ | $\begin{gathered} \mathrm{PO} \\ 8 \end{gathered}$ | $\begin{array}{\|c\|c\|} \hline \mathrm{PO} & \mathrm{PO} \\ 9 & 10 \\ \hline \end{array}$ |  | $\begin{array}{\|c\|} \hline \mathrm{PO} \\ 12 \end{array}$ |  |  | $\begin{gathered} \text { Lev } \\ \text { el } \end{gathered}$ |
| 1 | 18MAT41.1 | Apply the knowledge of complex analysis its properties and construction of analytical functions. |  |  |  |  |  |  |  | 2.5 | 2.52.5 |  | 2.5 |  |  | L3 |
| 2,4 | 18MAT41.2 | Analyze various transformations to convert one plane to another evaluate complex integral and finding the bet relation between the variables. | 2.5 |  | 2.5 |  |  |  |  | 2.5 | 2.52.5 |  | 2.5 |  |  | $\begin{gathered} \text { L3\& } \\ \text { L4 } \end{gathered}$ |
| 3 | 18MAT41.3 | Learn different probability measures , distribution function and its properties and also apply various inequalities in statistical analysis. |  |  |  |  |  |  |  |  | $2.52 .5$ |  | 2.5 |  |  | L3 |



## 5. Curricular Gap and Content

Topics \& contents not covered (from A.4), but essential for the course to address POs and PSOs.

| Mod <br> ules | Gap Topic | Actions Planned | Schedule Planned | Resources Person | PO Mapping |
| :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |

## 6. Content Beyond Syllabus

Topics \& contents required (from A.5) not addressed, but help students for Placement, GATE, Higher Education, Entrepreneurship, etc.

| Mod <br> ules | Gap Topic | Area | Actions Planned | Schedule <br> Planned | Resources <br> Person | PO Mapping |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |

## C. COURSE ASSESSMENT

## 1. Course Coverage

Assessment of learning outcomes for Internal and end semester evaluation. Distinct assignment for each student. 1 Assignment per chapter per student. 1 seminar per test per student.

| Mod ules | Title | Teach. Hours | No. of question in Exam |  |  |  |  |  | CO | Levels |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | CIA-1 | CIA-2 | CIA-3 | Asg | Extra Asg | SEE |  |  |
| 1 | Calculus of complex function | 10 | 2 | - | - |  |  | 2 | CO1 | L3 |
| 2 | Conformal transformation\&complex integration | 10 | 2 | - | - |  |  | 2 | CO 2 | L4 |
| 3 | probability | 10 | - | 2 | - |  |  | 2 | CO 3 | L3 |
| 4 | Curve fitting\&staistical methods | 10 | - | 2 | - |  |  | 2 | CO 2 | L3 |
| 5 | Joint probability\&sampling theory | 10 | - | - | 4 |  |  | 2 | CO 5 | L3 |
| - | Total | 50 | 4 | 4 | 4 |  |  | 10 | - | - |

## 2. Continuous Internal Assessment (CIA)

Assessment of learning outcomes for Internal exams. Blooms Level in last column shall match with A.2.

| Mod <br> ules | Weightage in <br> Marks | CO | Levels |  |
| :---: | :---: | :---: | :---: | :---: |
| 1,2 | ClA Exam -1 | 30 | $\mathrm{CO} 2, \mathrm{CO} 3$, | $\mathrm{L}, \mathrm{L} 3$ |
| 3,4 | CIA Exam -2 | 30 | $\mathrm{CO}, \mathrm{CO} 4$ | $\mathrm{~L} 3, \mathrm{~L} 3$ |
| 5 | CIA Exam -3 | 30 | CO 2 | L 4 |
|  |  |  |  |  |
| 1,2 | Assignment -1 | 10 | $\mathrm{CO} 2, \mathrm{CO} 3$, | $\mathrm{L} 3, \mathrm{~L} 3$ |

COURSE PLAN - CAY 2019-20


## D1. TEACHING PLAN - 1

## Module - 1

| Title: | Calculu of complex functions: | Appr Time: | 12 Hrs |
| :---: | :---: | :---: | :---: |
| a | Course Outcomes | CO | Blooms |
| - | The student should be able to: | - | Level |
| 1 | Apply the knowledge of complex analysis its properties and construction of analytical functions | CO1 | L3 |
| b | Course Schedule | - | - |
| Class No | Portion covered per hour | - | - |
| 1 | Complex Variables: Review of a function of a complex variable, limits, continuity, differentiability. Analytic functions-Cauchy-Riemann equations in cartesian and polar forms. Properties and construction of analytic functions | C01 | L3 |
| 2 | Function of a complex variables | C01 | L3 |
| 3 | Analytic functions problems\& theorems | C01 | L3 |
| 4 | Cauchy-Riemann equations in cartesian form | C01 | L3 |
| 5 | Cauchy-Riemann equations in polar forms | C01 | L3 |
| 6 | Harmonic property | C01 | L3 |
| 7 | Cauchy' theorems | C01 | L3 |
| 8 | Consequence of cauchy's theorem | C01 | L3 |
| 9 | Construction of analytic function | C01 | L3 |
| 10 | Milne thomon method problems | C01 | L3 |
|  |  |  |  |
| c | Application area; |  |  |
| 1 | To study the nature of electromagnetic wave in conductors.. | co1 | L3 |
|  |  |  |  |
|  |  |  |  |
| d | REVIEW QUESTIONS: |  |  |
| 1 | Derive the Cauchy Riemanns equation in the Cartesian form. | co1 | L3 |
| 2 | Derive Cauchy Riemann equations in Polar form. <br> (OR) <br> Derive the necessary conditions for $\mathrm{f}(\mathrm{z})=\mathrm{u}(\mathrm{r}, \theta)+\mathrm{iv}(\mathrm{r}, \theta)$ to be analytic in a regio | co1 | L3 |
| 3 | Show that $\mathrm{Z}^{\mathrm{n}}$ is analytic . Hence find its derivative | co1 | L3 |
| 4 | If $w=z^{3}$ find $d w / d z$. | co1 | L3 |


| 5 | If $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$ is analytic and hence find $\mathrm{f}(\mathrm{z})$ if $\mathrm{u}-\mathrm{v}=(\mathrm{x}-\mathrm{y})\left(x^{2}+4 x y+y^{2}\right)$. | co1 | L3 |
| :---: | :---: | :---: | :---: |
| 6 | Find the analytic function $\mathrm{u}+\mathrm{iv}$ where u is given to be $\mathrm{u}=\mathrm{e}^{\mathrm{x}}\left(\left(x^{2}-y^{2}\right)\right.$ cosy2xysiny) | CO1 | L3 |
| 7 | If $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$ is analytic prove that $\left(\frac{\partial^{2}}{\partial x^{2}}+\frac{\partial^{2}}{\partial x^{2}}\right)\|f(z)\|^{2}=4\left\|f^{I}(z)\right\|^{2}$ | co1 | L3 |
| 8 | If $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$ is analytic function, show that $\left[\frac{\partial}{\partial x}\|f(Z)\|\right]^{2}+\left[\frac{\partial}{\partial y}\|f(Z)\|\right]^{2}=\left\|f^{I}(Z)\right\|^{2}$. | co1 | L3 |
| 9 | Find the analytic function $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$ given that $\left.\mathrm{u}=\mathrm{z}_{\mathrm{z}}\right)+\frac{x}{\left(x^{2}+y^{2}\right)}$. | co1 | L3 |
| 10 | If $f(z)=u(r, \theta)+i v(r, \theta)$ is an analytic function, show that $u$ and $v$ satisfy yhe equation $\frac{\partial^{2} \phi}{\partial r^{2}}+\frac{1}{r} \frac{\partial \phi}{\partial r}+\frac{1}{r^{2}} \frac{\partial^{2} \phi}{\partial \theta^{2}}=0$ | co1 | L3 |
| 11 | Find the analytic function $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$ whose real part is $y+e^{x}$ cosy . | co1 | L3 |
|  |  |  |  |
|  |  |  |  |
| e | Experiences |  |  |

Module - 2

| Title: | Conformal tranformation \& comple integration: | Appr Time: | 7 Hrs |
| :---: | :---: | :---: | :---: |
| a | Course Outcomes | CO | Blooms |
|  | The student should be able to: | - | Level |
| 1 | Analyze various transformations to convert one plane to another evaluate complex integral and finding the bet relation between the variables. | co2 | L3 \& L4 |
| b | Course Schedule | - | - |
| Class No | Portion covered per hour | - | - |
| 1 | Conformal transformation introduction | co2 | L3 \& L4 |
| 2 | Discussion of transformations: $\mathrm{W}=z^{\wedge}$ 2 | co2 | L3 \& L4 |
| 3 | Discussion of transformations: $\mathrm{W}=\mathrm{e}^{\wedge} \mathrm{Z}$ | co2 | L3 \& L4 |
| 4 | Discussion of transformations: $\mathrm{W}=\mathrm{Z}+1 / \mathrm{Z}$ | co2 | L3 \& L4 |
| 5 | Bilinear transformation problems | co2 | L3 \& L4 |
| 6 | Complex integration introduction | co2 | L3 \& L4 |
| 7 | Line function integral of a complex | $\mathrm{co2}$ | L3 \& L4 |
| 8 | cauchy's theorem | co2 | L3 \& L4 |
| 9 | cauchy's integral formmula | co2 | L3 \& L4 |
| 10 | Baed on problems | co2 | L3 \& L4 |
|  |  |  |  |
| c | Application Areas | - | - |
| 1 | To study the nature of complex potential in field theory Curve fitting is the process of constructing a curve that has the best fit to a series of data points. | CO2 | L3\&L4 |
|  |  |  |  |
|  |  |  |  |
| d | Review Questions | - | - |
| - |  | - | - |
| 1 | Discussion of transformations: $\mathrm{W}=z^{\wedge}$ 2 | $\mathrm{co2}$ | L4 |
| 2 | Discussion of transformations: $W=\mathrm{e}^{\wedge} \mathrm{Z}$ | O2 | L4 |
| 3 | Discussion of transformations: $\mathrm{W}=2+1 / Z$ | co2 | L4 |
| 4 | Find the bilinear transformation that maps the points $\mathrm{z}=-1, \mathrm{i}, 1$ on to the points w=1,i,-1 respectively. | co2 | L3 |
| 5 | Find the bilinear transformation that maps the points 1,i,-1 onto the points i, , , -1 | co2 | L3 |

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|  | respectively |  |  |
| :---: | :---: | :---: | :---: |
| 6 | Find the bilinear transformation that transforms the points $z 1=1, z 2=i, z 3=-1$ onto <br> the points $W 1=2, W 2=i, W 3=-2$ find the fixed points of the transformation. | $\mathrm{co2}$ | L 3 |
| 7 | Line function, complex line integrals | $\mathrm{co2}$ | L 3 |
| 8 | cauchy's theorem | co 2 | L 3 |
| 9 | cauchy's integral formmula | $\mathrm{co2}$ | L 3 |
| 10 | Baed on problems | $\mathrm{co2}$ | L 3 |
| $\mathbf{e}$ | Experiences | - | - |
| 1 |  |  |  |

## E1. CIA EXAM - 1

## a. Model Question Paper - 1



## b. Assignment -1

Note: A distinct assignment to be assigned to each student.

$|$| Model Assignment Questions |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Crs Code: | 18MAT41 | Sem: | 4 | Marks: | 5 | Time: |
| Course: | Complexanalysis, probability\&stastistialmetho <br> ds | Module : 1, 2 |  |  |  |  |
| Note: Each student to answe5r 2-3 assignments. Each assignment carries equal mark. |  |  |  |  |  |  |
| SNo USN | Assignment Description | Marks | CO | Level |  |  |


|  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| 1 | Derive the Cauchy Riemanns equation in the Cartesian form. | 5 | CO1 | L3 |
| 2 | Derive Cauchy Riemann equations in Polar form. <br> (OR) <br> Derive the necessary conditions for $f(z)=u(r, \theta)+i v(r, \theta)$ to be analytic in a regio | 5 | CO1 | L3 |
| 3 | Show that $\mathrm{Z}^{\mathrm{n}}$ is analytic . Hence find its derivative | 5 | CO1 | L3 |
| 4 | If $w=z^{3}$ find dw/dz. | 5 | CO1 | L3 |
| 5 | If $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$ is analytic and hence find $\mathrm{f}(\mathrm{z})$ if $\mathrm{u}-\mathrm{v}=(\mathrm{x}-\mathrm{y})($ $\left.x^{2}+4 x y+y^{2}\right)$. | 5 | CO1 | L3 |
| 6 | Find the analytic function $\mathrm{u}+\mathrm{iv}$ where u is given to be $\mathrm{u}=\mathrm{e}^{\mathrm{x}}(($ $\left.\left.x^{2}-y^{2}\right) \cos y-2 x y \sin y\right)$ | 5 | CO1 |  |
| 7 | If $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$ is analytic prove that $\left.\left(\frac{\partial^{2}}{\partial x^{2}}+\frac{\partial^{2}}{\partial x^{2}}\right)\left\|f(z)^{2}=4\right\| f^{I}(z)\right\|^{2}$ | 5 | CO1 | L3 |
| 8 | If $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$ is analytic function, show that $\left[\frac{\partial}{\partial x}\|f(Z)\|\right]^{2}+\left[\frac{\partial}{\partial y}\|f(Z)\|\right]^{2}=\left\|f^{I}(Z)\right\|^{2}$. | 5 | CO1 | L3 |
| 9 | Find the analytic function $f(z)=u+i v$ given that $u=i i)+$ $\frac{x}{\left(x^{2}+y^{2}\right)}$. | 5 | CO1 | L3 |
| 10 | If $f(z)=u(r, \theta)+i v(r, \theta)$ is an analytic function, show that $u$ and $v$ satisfy yhe equation $\frac{\partial^{2} \phi}{\partial r^{2}}+\frac{1}{r} \frac{\partial \phi}{\partial r}+\frac{1}{r^{2}} \frac{\partial^{2} \phi}{\partial \theta^{2}}=0$ | 5 | CO1 | L3 |
| 11 | Find the analytic function $\mathrm{f}(\mathrm{z})=\mathrm{u}+\mathrm{iv}$ whose real part is $y+e^{x} \cos y$. | 5 | CO1 | L3 |
| 12 | Discussion of transformations:W $=z^{\wedge} 2$ | 5 | CO 2 | L4 |
| 13 | Discussion of transformations: $\mathrm{W}=\mathrm{e}^{\wedge} \mathrm{Z}$ | 5 | CO 2 | L4 |
| 14 | Discussion of transformations: $W=Z+1 / Z$ | 5 | CO 2 | L4 |
| 15 | Find the bilinear transformation that maps the points $z=-1, i, 1$ on to the points $W=1, i,-1$ respectively. | 5 | CO 2 | L4 |
| 16 | Find the bilinear transformation that maps the points $1, \mathrm{i},-1$ onto the points i,o,-1 respectively | 5 | CO 2 | L4 |
| 17 | Find the bilinear transformation that transforms the points $z 1=1, z 2=i, z 3=-1$ onto the points $w 1=2, w 2=i, w 3=-2$ find the fixed points of the transformation. | 5 | CO 2 | L4 |
| 18 | Line function, complex line integrals | 5 | CO 2 | L4 |
| 19 | cauchy's theorem | 5 | CO 2 | L4 |
| 20 | cauchy's integral formmula | 5 | CO 2 | L4 |
| 21 | Baed on problems | 5 | CO 2 | L4 |
| 22 | P.T $W=1+z / 1-z$ map the region $\|z\|$ less than are equal to 1 onto the half plane $R(U)$ greaterthan are equal to o being the region ugreater than are equal to 0 | 5 | CO 2 | L4 |
| 23 | Find the invariant points of the following bilinear transformations $W=z-1-i / z+2$ | 5 | CO 2 | L4 |
| 24 | Bilinear transformationw=3z-4/z-1 | 5 | CO 2 | L4 |
| 25 | Obtain the image of the region bounded by the line $x=1, x=2, y=1, y=2$ under the tranformation $w=e^{\wedge} z$ and sketch the | 5 | CO 2 | L4 |


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| :--- | :--- | :--- | :--- | :--- |

## D2. TEACHING PLAN - 2

## Module - 3

| Title: | PROBABILITY DISTRIBUTIONS: | Appr Time: | 12 Hrs |
| :---: | :---: | :---: | :---: |
| a | Course Outcomes | CO | Blooms |
| - | The student should be able to: | - | Level |
| 1 | Learn different probability measures, distribution function and its properties and also apply various inequalities in statistical analysis. | $\mathrm{CO}_{3}$ |  |
|  |  |  |  |
|  |  |  |  |
| b | Course Schedule |  |  |
| Class No | Portion covered per hour | - | - |
| 1 | Probability distributions: Introduction on probability some examples | $\mathrm{CO}_{3}$ | L3 |
| 2 | Random variables(discrete and continuous) | $\mathrm{CO}_{3}$ | L3 |
| 3 | probability mass/density function | $\mathrm{CO}_{3}$ | L3 |
| 4 | Binomial distribution based on problems | $\mathrm{CO}_{3}$ | L3 |
| 5 | poisson distribution based on problems | $\mathrm{CO}_{3}$ | L3 |
| 6 | Exponential ditribution and problems normal | $\mathrm{CO}_{3}$ | L3 |
| 7 | normal distribution\& problems. | $\mathrm{CO}_{3}$ | L3 |
| 8 | More examples on dirtibutions | $\mathrm{CO}_{3}$ | L3 |
| c | Application Areas | - | - |
| - |  | - | - |
| 1 | To analyze problems associated with optimization of digital circuits | co3 | L3 |
|  |  |  |  |
|  |  |  |  |
| d | Review Questions | - | - |
| - |  | - | - |
| 1 | Find the binomial probability distribution which has mean 2 and variance 4/3 |  |  |
| 2 | Fit a poiSSon distribution for the following data and calculate the theoretical frequency $\begin{array}{llllll} \mathrm{X}: 0 & 1 & 2 & 3 & 4 \\ \\ \mathrm{Y}: 122 & 60 & 15 & 2 & 1 \end{array}$ |  |  |
| 3 | The number of telephone lines busy at an instant of time is binomial variate with probability 0.1 that a line is busy. If 10 lines are chosen at random, what is the probability that i) No line is busy ii) At least 5 lines are busy iii) At most 3 lines are busy. | $\mathrm{CO}_{3}$ | L3 |
| 4 | The probability that a man aged 60 will live up to 70 is 0.65 . Out of 10 men, now at the age of 60 ,find probability that 1)Atlest 7 will live up ) 2) Exactly 9 will Live up to 7 | $\mathrm{CO}_{3}$ | L3 |
| 5 | The probability that a man aged 60 will live up to 70 is 0.65 . Out of 10 men, now at the age of 60 ,find probability that 1)Atlest 7 will live up ) 2) Exactly 9 will Live up to 7 | $\mathrm{CO}_{3}$ | L3 |
| 6 | In sampling a large number of parts manufactured by a company , the mean number of defectives in a samples of 20 is 2 . Out of 1000 such | $\mathrm{CO}_{3}$ | L3 |


|  | samples, how many would be expected to contain atleast three defective parts |  |  |
| :---: | :---: | :---: | :---: |
| 7 | Given that $2 \%$ of the fuses manufactured by a firm are defective ,find by using Poisson distribution ,the probability that a box containing 200 fuses has <br> i)No defective fuses ii) 3 or more defective fuses iii)At least one defective fuse. | CO 3 | L3 |
| 8 | For the following normal distribution find c and also the mean and S.D of frequency distribution | CO 3 | L3 |
| 9 | In normal distribution $31 \%$ of the items are under 45 and $8 \%$ are over 64 . Find the mean and standard deviation given that $\mathrm{A}(0.5)-0.19$ And $\mathrm{A}(1.4)=0.42$ | CO 3 | L3 |
| 10 | i) A die is thrown 8times. Find the probability that ' 3 ' falls <br> ii) Exactly 2 times <br> iii) At least once <br> At the most 7times | CO 3 | L3 |
| 11 | In certain town the duration of shower has mean 5 minutes. What is the probability that shower will last for i) 10 minutes or more ii) less than 10 minutes iii) between 10 and 12 minutes | CO 3 | L3 |
| 12 | If $x$ I a normal variate with mean 30 and S.D 5 find the probability that (1) 26 less than are equal to"" $X$ '"Less than are equal to 40 (2) $X$ greater than are equal to 45 . | CO 3 | L3 |
| e | Experiences | - | - |
| 1 |  |  |  |
| 2 |  |  |  |

Module - 4

| Title | Curve fitting \& statistical methods | Appr <br> Time: | 13 Hrs |
| :---: | :--- | :---: | :---: |
| $\mathbf{a}$ | Course Outcomes | CO | Blooms |
| - | Student should be able to |  | LEVEL |
| 1 | Analyze various transformations to convert one plane to another evaluate <br>  <br> Apply to construct numerical data and solving by least square method | $\mathrm{co2}$ | L3 |
| $\mathbf{b}$ | Course Schedule |  |  |
| Class No | Portion covered per hour | - | - |
| 1 | Correlation and rank correlation problems | $\mathrm{co2}$ | L 3 |
| 2 | More examples on rank correlation | $\mathrm{co2}$ | L 3 |
| 3 | Regression and Regression coefficients | $\mathrm{co2}$ | L 3 |
| 4 | lines of regression - problems | $\mathrm{co2}$ | L 3 |
| 5 | Regression line XON Y \&Y ON X problems | $\mathrm{co2}$ | L 3 |
| 6 | Fitting of curves introduction- Fitting equation of straight line. | $\mathrm{co2}$ | L 3 |
| 7 | Fitting equation of parabola. | $\mathrm{co2}$ | L 3 |
| 8 | Second degree parabola problems | $\mathrm{co2}$ | L 3 |
| 9 | Fitting equation of exponential curve problems | $\mathrm{co2}$ | L 3 |
| 10 | More examples |  |  |
|  |  | - | - |
| $\mathbf{c}$ | Application Areas | - | - |
| - | Students should be able employ / apply the Module learnings to ... |  |  |


| 1 | To study the nature of complex potential in field theory Curve fitting is the process of constructing a curve that has the best fit to a series of data points. | CO2 | L3 |
| :---: | :---: | :---: | :---: |
|  |  |  |  |
|  |  |  |  |
| d | Review Questions | - | - |
| - |  |  |  |
| 1 | Fit a curve of the form $\mathrm{y}=\mathrm{a} e^{b x}$ to the following data : | CO 2 | L3 |
| 2 | Fit a parabola by using least squares method to the following method to the following data $\begin{array}{lrrrrrrr} \mathrm{x}: & 1.0 & 1.5 & 2.0 & 2.5 & 3.0 & 3.5 & 4.0 \\ \mathrm{y}: & 1.1 & 1.3 & 1.6 & 2.0 & 2.7 & 3.4 & 4.1 \end{array}$ | CO 2 | L3 |
| 3 | Fit a traight line $\mathrm{y}=\mathrm{ax}+\mathrm{b}$ for the following data x:1346891114 Y:12445789 | CO 2 | L3 |
| 4 | Fit a straight line in the leat quare ence for the following data $\begin{aligned} & \mathrm{X}: 5070100120 \\ & \mathrm{Y}: 12152125 \end{aligned}$ | CO 2 | L3 |
| 5 | Fit a second degree parabola $y=a x^{\wedge} 2+b x+c$ in the leat square sence for the following data $\begin{array}{lccccc} \mathrm{X}: 1 & 2 & 3 & 4 & 5 \\ \mathrm{Y}: 10 & 12 & 13 & 16 & 19 & \end{array}$ | CO 2 | L3 |
| 6 | Fit a curve of the form $y=a e^{\wedge} b x$ for the data $\begin{array}{lcc} \mathrm{X}: 0 & 2 & 4 \\ \mathrm{Y}: 8.12 & 12 & 31.82 \end{array}$ | CO 2 | L3 |
| 7 | Compute the coefficient of correlation and the equation of the lines of regression for the data $\begin{array}{lllllllll} \mathrm{X}: 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \mathrm{Y}: 9 & 8 & 10 & 12 & 11 & 13 & \\ 14 \end{array}$ | CO 2 | L3 |
| 8 | Obtain the line of regresion andf hence find the coefficient of correlation for the data $\begin{array}{lllllll} \mathrm{X}: 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \mathrm{Y}: 9 & 8 & 10 & 12 & 11 & 13 & 14 \end{array}$ | CO 2 | L3 |
| 9 | Find the correlation coefficient for the data $\begin{array}{llllllllll} \mathrm{A}: 92 & 89 & 87 & 86 & 83 & 77 & 71 & 63 & 53 & 50 \\ \mathrm{Y}: 86 & 83 & 91 & 77 & 68 & 85 & 52 & 82 & 37 & 57 \end{array}$ | CO 2 | L3 |
| 10 | Compute the rank correlation coefficient for the followingdata $\begin{array}{llllllllll} \mathrm{x}: 68 & 64 & 75 & 50 & 64 & 80 & 75 & 40 & 55 & 64 \\ \mathrm{y}: 62 & 58 & 68 & 45 & 81 & 60 & 68 & 48 & 50 & 70 \end{array}$ | CO 2 | L3 |

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|  | Experiences |  |  |
| :---: | :--- | :---: | :---: |
| $\mathbf{e}$ |  | - | - |
| 1 |  |  |  |

E2. CIA EXAM - 2
a. Model Question Paper - 2
Crs Code:18MAT41 Sem: IV $\quad$ Marks: 30 |Time: 75 minutes

Course: Complexanalysis,probability\&stastistialmethods

| - | - | Note: Answer all questions, each carry equal marks. Module : 3, 4 | Marks | CO | Level |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | a | Find the binomial probability distribution which has mean 2 and variance $4 / 3$ | 5 | $\mathrm{CO}_{3}$ | L3 |
|  | b | Fit a poion distribution for the following data and calculate the theoretical frequency $\begin{array}{llllll} \mathrm{X}: 0 & 1 & 2 & 3 & 4 \\ \mathrm{Y}: 122 & 60 & 15 & 2 & 1 \end{array}$ | 5 | CO 3 | L3 |
|  | C | The number of telephone lines busy at an instant of time is binomial variate with probability 0.1 that a line is busy. If 10 lines are chosen at random, what is the probability that i) No line is busy ii) At least 5 lines are busy iii) At most 3 lines are busy. |  |  | L3 |
|  |  |  | 5 | $\mathrm{CO}_{3}$ | L3 |
|  |  | OR |  |  |  |
| 2 | a | Given that 2\% of the fuses manufactured by a firm are defective ,find by using Poisson distribution ,the probability that a box containing 200 fuses has <br> i)No defective fuses ii) 3 or more defective fuses iii)At least one defective fuse. | 5 | $\mathrm{CO}_{3}$ | L3 |
|  | b | Obtain the mean and S.D of the normal distribution. | 5 | $\mathrm{CO}_{3}$ | L3 |
|  | c | In a normal ditribution $31 \%$ of the itemes are under 45 and $8 \%$ of the item are over 64.find the mean and S.D of the distributions | 5 | $\mathrm{CO}_{3}$ | L3 |
| 3 | a | Fit a parabola by using least squares method to the following method to the following data : $\begin{array}{llllllll} \mathrm{x}: & 1.0 & 1.5 & 2.0 & 2.5 & 3.0 & 3.5 & 4.0 \\ \mathrm{y}: & 1.1 & 1.3 & 1.6 & 2.0 & 2.7 & 3.4 & 4.1 \end{array}$ | 5 | CO 2 | L3 |
|  | b | Fit a traight line $\mathrm{y}=\mathrm{ax}+\mathrm{b}$ for the following data $\mathrm{x}: 1346891114$ <br> Y:12445789 | 5 | CO 2 | L3 |
|  | c | Fit a curve of the form $y=a e^{\wedge} b x$ for the data $\begin{array}{lccc}\mathrm{X}: & 0 & 2 & 4 \\ \mathrm{Y}: 8 & 12 & 12 & 31.82\end{array}$ <br> Y:8.12 1231.82 | 5 | CO 2 | L3 |
|  |  | OR |  |  |  |
| 4 | a | Find the correlation coefficient for the data A:92 $8987 \quad 8683 \quad 77 \begin{array}{llllll}71 & 63 & 53 & 50\end{array}$ Y:86 $83 \begin{array}{lllllllll}91 & 77 & 68 & 85 & 52 & 82 & 37 & 57\end{array}$ | CO2 | L3 | L3 |



## b. Assignment - 2

Note: A distinct assignment to be assigned to each student.

| Model Assignment Questions |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Crs Code | 18MAT41 Sem: |  | IV | Marks: |  | 10 | Time: |  |  |  |  |
| Course: | Complexanalysis,probability\&stastistialmetho ds |  |  |  |  | Module : 3.4 |  |  |  |  |  |
| Note: Each student to answer 2-3 assignments. Each assignment carries equal mark |  |  |  |  |  |  |  |  |  |  |  |
| SNo | USN | Assignment Description |  |  |  |  |  |  | Marks | CO | Level |
| ${ }^{1}$ |  | The pdf of a variate x is given by the following table: |  |  |  |  |  |  | 5 | CO 3 |  |
|  |  | $X$ 0 1 2 3 <br> $P(x)$ $k$ $3 k$ $5 k$ $7 k$ <br> For what value of $k$ this represents a valid probability distribution? |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |
| 2 |  | Fit a poiSSon distribution for the following data and calculate the theoretical frequency$\begin{array}{llllll} \mathrm{X}: 0 & 1 & 2 & 3 & 4 \\ \\ \mathrm{Y}: 122 & 60 & 15 & 2 & 1 \\ \hline \end{array}$ |  |  |  |  |  |  | 5 | $\mathrm{CO}_{3}$ | L3 |
| 3 |  | When a coin is tossed 4 time find the probability of gettinh 1) exactly one head 2)atmot 3 head 3) at mot 2 heads |  |  |  |  |  |  | 5 | $\mathrm{CO}_{3}$ | L3 |
| 4 |  | The number of telephone lines busy at an instant of time is binomial variate with probability 0.1 that a line is busy. If 10 lines are chosen at random, what is the probability that i) No line is busy ii) At least 5 lines are busy iii) At most 3 lines are busy. |  |  |  |  |  |  | 5 | $\mathrm{CO}_{3}$ | L3 |
| 5 |  | Given that $2 \%$ of the fuses manufactured by a firm are defective, find by using Poisson distribution ,the probability that a box containing 200 fuses has i)No defective fuses ii) 3 or more defective fuses iii)At least one defective fuse. |  |  |  |  |  |  | 5 | CO 3 | L3 |
| 6 |  | The probability that a man aged 60 will live up to 70 is 0.65 . Out of 10 men, now at the age of 60 ,find probability that <br> 1)Atlest 7 will live up ) 2)Exactly 9 will live up to 7 |  |  |  |  |  |  | CO 3 | L3 | L3 |
| 7 |  | In sampling a large number of parts manufactured by a company, the mean number of defectives in a samples of 20 is 2 . Out of 1000 such samples, how many would be expected to contain atleast three defective parts |  |  |  |  |  |  | CO 3 | L3 | L3 |
| 8 |  | 5In normal distribution 31\% of the items are under 45 and |  |  |  |  |  |  | 5 | CO3 | L3 |


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| :---: | :---: | :---: | :---: | :---: |
|  | $8 \%$ are over 64 .Find the mean and standard deviation given that $\mathrm{A}(0.5)-0.19 \mathrm{~A}$ nd $\mathrm{A}(1.4)=0.42$ |  |  |  |
| 9 | 1. A die is thrown 8times. Find the probability that ' 3 ' falls <br> 2. Exactly 2 times <br> 3. At least once At the most 7times | 5 | CO 3 | L3 |
| 10 | In certain town the duration of shower has mean 5 minutes. What is the probability that shower will last for i) 10 minutes or more ii) less than 10 minutes iii) between 10 and 12 minutes | 5 | CO 3 | L3 |
| 11 | The probability that a pen manufactured by a company will be defective is 0.1 . if 12 such pens are selected, find the probability that i) exactly 2 will be defective ii) at least 2 will be defective iii) none will be defective. | 5 | CO 3 | L3 |
| 12 | In a normal ditribution $31 \%$ of the itemes are under 45 and $8 \%$ of the item are over 64.find the mean and S.D of the distributions | 5 | co3 | L3 |
| 13 | If $\times$ I a normal variate with mean 30 and S.D 5 find the probability that (1) 26 less than are equal to"" X'"Less than are equal to40 (2) $X$ greater than are equal to 45 . | 5 | co3 | L3 |

## D3. TEACHING PLAN - 3

Module - 5

| Title: | Joint probability distribution \& sampling theory | Appr Time: | 10 Hrs |
| :---: | :---: | :---: | :---: |
| a | Course Outcomes | CO | Blooms |
| - | The student should be able to: | - | Level |
| 1 | To solve problems related to information and coding theory\&To smoothen and prediction of discrete data in digital computers \& cruise control system in motor vehicles. | CO4 | L3 |
|  |  |  | L3 |
| b | Course Schedule | - | - |
| $\begin{aligned} & \text { Class } \\ & \text { No } \end{aligned}$ | Portion covered per hour | - | - |
| 1 | Introduction on joint probability distribution | CO4 | L3 |
| 2 | joint probability distribution for two discrete random variables | co4 | L3 |
| 3 | Problems based on expectations | CO4 | L3 |
| 4 | Problems on co variance | CO4 | L3 |
| 5 | Sampling theory: Introduction to sampling distributions, | CO4 | L3 |
| 6 | standard error,,test of hypothesis for means | CO4 | L3 |
| 7 | Type 1\&Type 2 errors | CO4 | L3 |
| 8 | Confidence limits for means students's t-distribution | CO4 | L3 |
| 9 | Chi-square distribution as a test of goodness of fit | CO4 | L3 |
| 10 | More examples on sampling theory | co4 | L3 |
|  |  |  |  |
|  |  |  |  |
| c | Application Areas | - | - |
| - | Students should be able employ / apply the Module learnings to | - | - |




## E3. CIA EXAM - 3

## a. Model Question Paper - 3



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## b. Assignment - 3

Note: A distinct assignment to be assigned to each student.

| Model Assignment Questions |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Crs Code: | 18 mat41 Sem: | IV | Marks: | 10 | Time: | $90-120$ minutes |
| Course: | Complexanalysis, probability\&stastistialmetho <br> ds | Module :5 |  |  |  |  |

Note: Each student to answer 2-3 assignments. Each assignment carries equal mark.

| SNo | USN | Assignment Description | Marks | CO | Level |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 1 |  | If the mean of an infinite population is 575 with standard deviation8.3,how large a sample must be used in order that there be one chance in 100 that the mean of the sample is less than 572 ? | 5 | CO 4 | L3 |
| 2 |  | Find the probability that in 100 tosses of a fair coin between $45 \%$ and $55 \%$ of the outcomes are heads | 5 | CO 4 | L3 |
| 3 |  | Out of 1000 samples of 200 children each in how many would you expect to find that 1 )iess than $40 \%$ are boys, 2 )between $40 \%$ and $60 \%$ are boys,3) $55 \%$ or more are girls | 5 | CO 4 | L3 |
| 4 |  | A random sample of 400 items chosen from an infinite population is found to have a mean of 82 and a standard deviation of 18 .find the $95 \%$ confidence limits for the mean of the population from which the sample is drawn | 5 | CO 4 | L3 |
| 5 |  | A biased coin is tossed 500 times and head turns up 120 times .find the $95 \%$ confidence limits for the proportion of heads turning up in infinitely many tosses | 5 | CO 4 | L3 |
| 6 |  | The S.D of the life-times of television tubes manufactured by a company is estimated as 100 hours. Find how large a sample must be taken in order to be $99 \%$ confident that the error in the estimated mean life-time will not exceed 20 hours | 5 | CO 4 | L3 |
| 7 |  | The S.D of the life-times of television tubes manufactured by a company is estimated as 100 hours. Find how large a sample must be taken in order to be $99 \%$ confident that the error in the estimated mean life-time will not exceed 20 hours | 5 | CO 4 | L3 |
| 8 |  | Find the students 't' for the following values in a sample of | 5 | CO 4 | L3 |



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## F. EXAM PREPARATION

## 1. University Model Question Paper





## 2. SEE Important Questions




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| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |
|  | e | Fit a second degree parabola $y=a x^{\wedge} 2+b x+c$ in the leat square sence for the following data $\begin{array}{lcccc} \mathrm{X}: 1 & 2 & 3 & 4 & 5 \\ \mathrm{Y}: 10 & 12 & 13 & 16 & 19 \end{array}$ |  | CO 2 | 2009 |
|  | f | Fit a curve of the form $\mathrm{y}=\mathrm{a} \mathrm{e}^{\wedge} \mathrm{bx}$ for the data $\begin{array}{lcc} \mathrm{X}: 0 & 2 & 4 \\ \mathrm{Y}: 8.12 & 12 & 31.82 \end{array}$ | 5 | CO 2 | 2010 |
|  | g | Compute the coefficient of correlation and the equation of the lines of regression for the data $\begin{array}{llllllll} \mathrm{X}: 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \mathrm{Y}: 9 & 8 & 10 & 12 & 11 & 13 & \\ 14 \end{array}$ | 5 | CO 2 | 2010 |
|  | h | Obtain the line of regresion andf hence find the coefficient of correlation for the data $\begin{array}{lllllll} \mathrm{X}: 1 & 2 & 3 & 4 & 5 & 6 & 7 \\ \mathrm{Y}: 9 & 8 & 10 & 12 & 11 & 13 & 14 \\ \hline \end{array}$ | 5 | CO 2 | 2010 |
|  | i | Find the correlation coefficient for the data $\begin{array}{llllllllll} \mathrm{A}: 92 & 89 & 87 & 86 & 83 & 77 & 71 & 63 & 53 & 50 \\ \mathrm{Y}: 86 & 83 & 91 & 77 & 68 & 85 & 52 & 82 & 37 & 57 \end{array}$ | 5 | CO 2 | 2013 |
|  | j | Compute the rank correlation coefficient for the followingdata | 5 | CO 2 | 2005 |
| 5 a | a | If the mean of an infinite population is 575 with standard deviation8.3, how large a sample must be used in order that there be one chance in 100 that the mean of the sample is less than 572 ? | 5 | CO 4 | 2016 |
|  | b | Find the probability that in 100 tosses of a fair coin between $45 \%$ and $55 \%$ of the outcomes are heads | 5 | CO 4 | 2015 |
|  | C | Out of 1000 samples of 200 children each in how many would you expect to find that 5 1)iess than $40 \%$ are boys,2)between $40 \%$ and $60 \%$ are boys, 3 ) $55 \%$ or more are girls | 5 | CO 4 | 2016 |
|  | d | A random sample of 400 items chosen from an infinite population is found to have a mean of 82 and a standard deviation of 18 .find the $95 \%$ confidence limits for the mean of the population from which the sample is drawn | 5 | CO 4 | 2009 |
|  | e | The mean and standard deviation of marks scored by a sample of 100 students are 67.45 and 2.92 find 1$) 95 \% 2) 99 \%$ confidence intervals for estimating the mean marks of the student population | 5 | CO 4 | 2008 |
|  | f | A biased coin is tossed 500 times and head turns up 120 times .find the $95 \%$ confidence limits for the proportion of heads turning up in infinitely many tosses | 5 | CO4 | 2012 |
|  | g | A biased coin is tossed 500 times and head turns up 120 times .find the $95 \%$ confidence limits for the proportion of heads turning up in infinitely many tosses | 5 | CO 4 | 2015 |
|  | h | A coin was tossed 400 times and the head turned up 216 times test the hypothesis that 5 the coin is unbiased at $5 \%$ level of significance./ |  | CO 4 | 2018 |
|  | i | Find how many heads in 64 tosses of a coin will ensure its fairness at 0.05 level of significance. | 5 | CO 4 | 2017 |
|  | j | F or a random sample of 16 values with mean 41.5 and the sum of the squares of the deviations from the mean equal to 135 and drawn from a normal population,find the $95 \%$ confidence limits and the confidence interval,for the mean of the mean of the population. | 5 | CO 4 | 2015 |
|  | k | Find the students ' t ' for the following values in a sample of eight:-4,-2,-5 $2,0,2,2,3,3$, taking the mean of the population to be zero |  | CO 4 | 2005 |

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## Course Outcome Computation

Academic Year:
Odd / Even semester

| INTERNAL TEST | T1 |  |  |  |  |  | T2 |  |  |  |  |  | T3 |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Course Outcome | CO1 |  | CO 2 |  | $\mathrm{CO}_{3}$ |  | CO 4 |  | CO 5 |  | CO6 |  | $\mathrm{CO7}$ |  | CO8 |  |
| QUESTION NO | Q1 | LV | Q2 | LV | Q3 | LV | Q1 | LV | Q2 | LV | Q3 | LV | Q1 | LV | Q2 | LV |
| MAX MARKS |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| USN-1 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| USN-2 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| USN-3 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| USN-4 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| USN-5 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| USN-6 |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Average CO Attainment |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |

LV Threshold : 3:>60\%, 2:>=50\% and <=60\%, 1: <=49\%
CO1 Computation : $(2+2+2+3) / 4=10 / 4=2.5$

## PO Computation



